



FIG. 1

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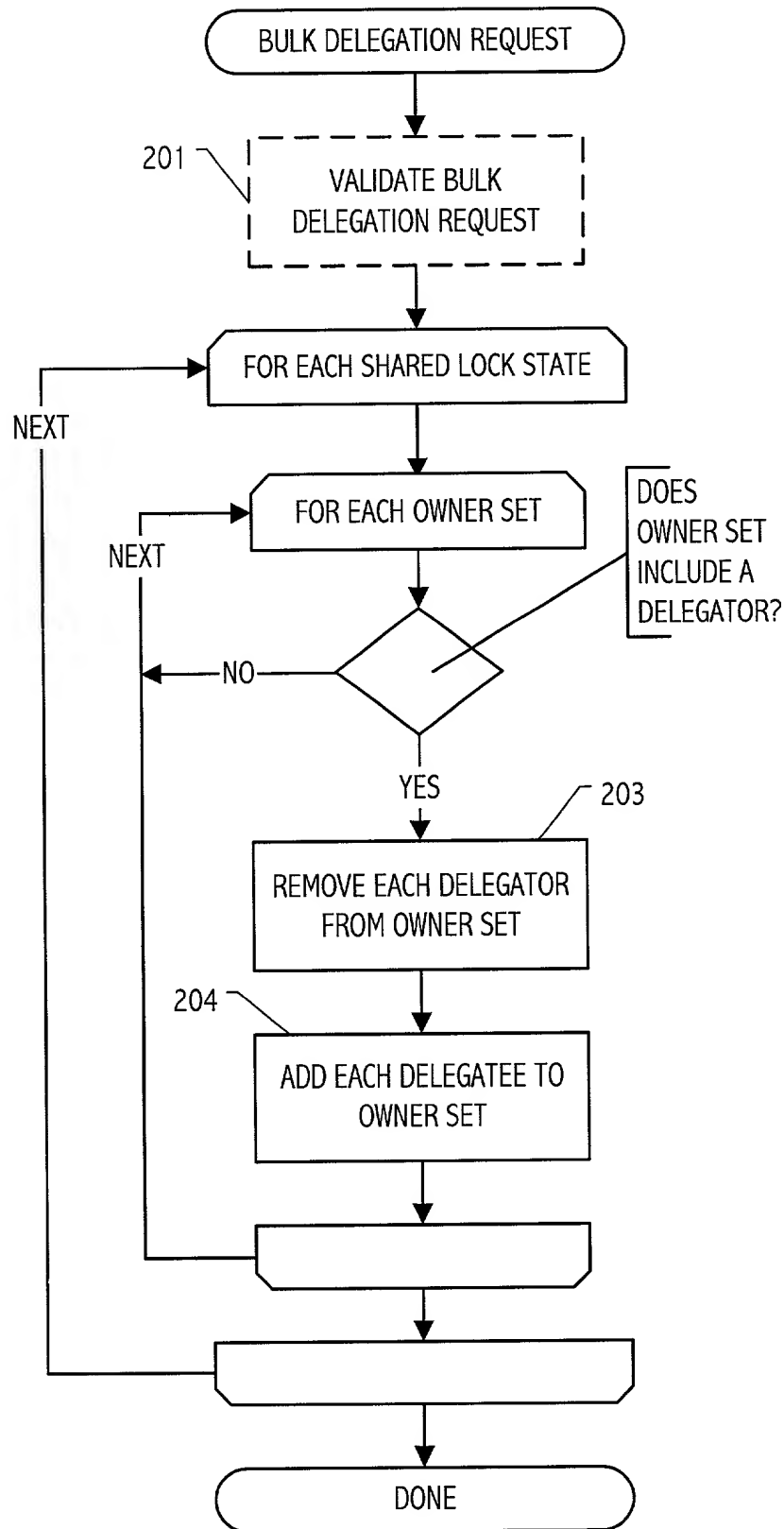


FIG. 2

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```

delegate(delegators, delegates)
begin
    foreach l in TSLS
        if  $\exists M, (delegators \cap Owners(l, M) \neq \emptyset) \wedge (\nexists M_i, M_i > M \wedge (delegators \cap Owners(l, M_i) \neq \emptyset))$ 
            TSLS.remove(l)
            // modify its owner set to reflect the effect of delegation
            foreach  $M_i, M_i \leq M$ 
                 $Owners(l, M_i) \leftarrow [Owners(l, M_i) - delegators] \cup delegates$ 
            end
            // does the new value duplicate an existing shared lock state ?
            if TSLS.contains(l)
                // yes. record the "original" being duplicated
                // and add the shared lock state to the set of duplicates.
                 $original(l) \leftarrow TSLS.get(l)$ 
                duplicates.add(l)
            else
                // no. Re-enter the modified shared lock in the TSLS.
                TSLS.add(l)
            endif
        endif
    end
    // Process duplicates now.
    foreach l in duplicates
        if  $\exists M, (delegators \cap Owners(l, M) \neq \emptyset) \wedge (\nexists M_i, M_i > M \wedge (delegators \cap Owners(l, M_i) \neq \emptyset))$ 
            // modify its owner set to reflect the effect of delegation
            foreach  $M_i, M_i \leq M$ 
                 $Owners(l, M_i) \leftarrow [Owners(l, M_i) - delegators] \cup delegates$ 
            end
        endif
    end
end
    
```

FIG. 3

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```
// Determine the validity of a delegating a lock set to the value l
boolean isValid(delegators, delegates, l)
begin
  if Owners(l, Write) =  $\emptyset$ 
    return true
  endif
  // at least one write lock owner
  if Owners(l, Write)  $\cap$  delegators =  $\emptyset$ 
    // All the delegators are read owners.
    // The delegation is valid if all delegates can ignore read-write
    // conflicts with the write owners.
    return  $\forall t \in \text{delegates}, \text{Owners}(l, \text{Write}) \subseteq \text{ICW}(t, rw)$ 
  endif
  // the lock is delegated in write mode – all delegates must ignore
  // write-write conflicts between each others and with each remaining
  // owners of the lock in write mode. Also, write-read conflicts should
  // be ignored with remaining owners of the lock in read mode.
  if |delegates| > 1
    // More than one delegatee
    if  $\exists t \in \text{delegates}, \exists c \in \{rw, wr, ww\}, \text{delegates} \not\subseteq \text{ICW}(t, c)$ 
      return false
    endif
  endif
  if  $\exists t \in \text{delegates}, (\text{Owners}(l, \text{Write}) - \text{delegators}) \not\subseteq \text{ICW}(t, ww)$ 
    return false
  endif
  if  $\exists t \in \text{delegates}, (\text{Owners}(l, \text{Read}) - \text{delegators}) \not\subseteq \text{ICW}(t, wr)$ 
    return false
  endif
  return true
end
```

FIG. 4

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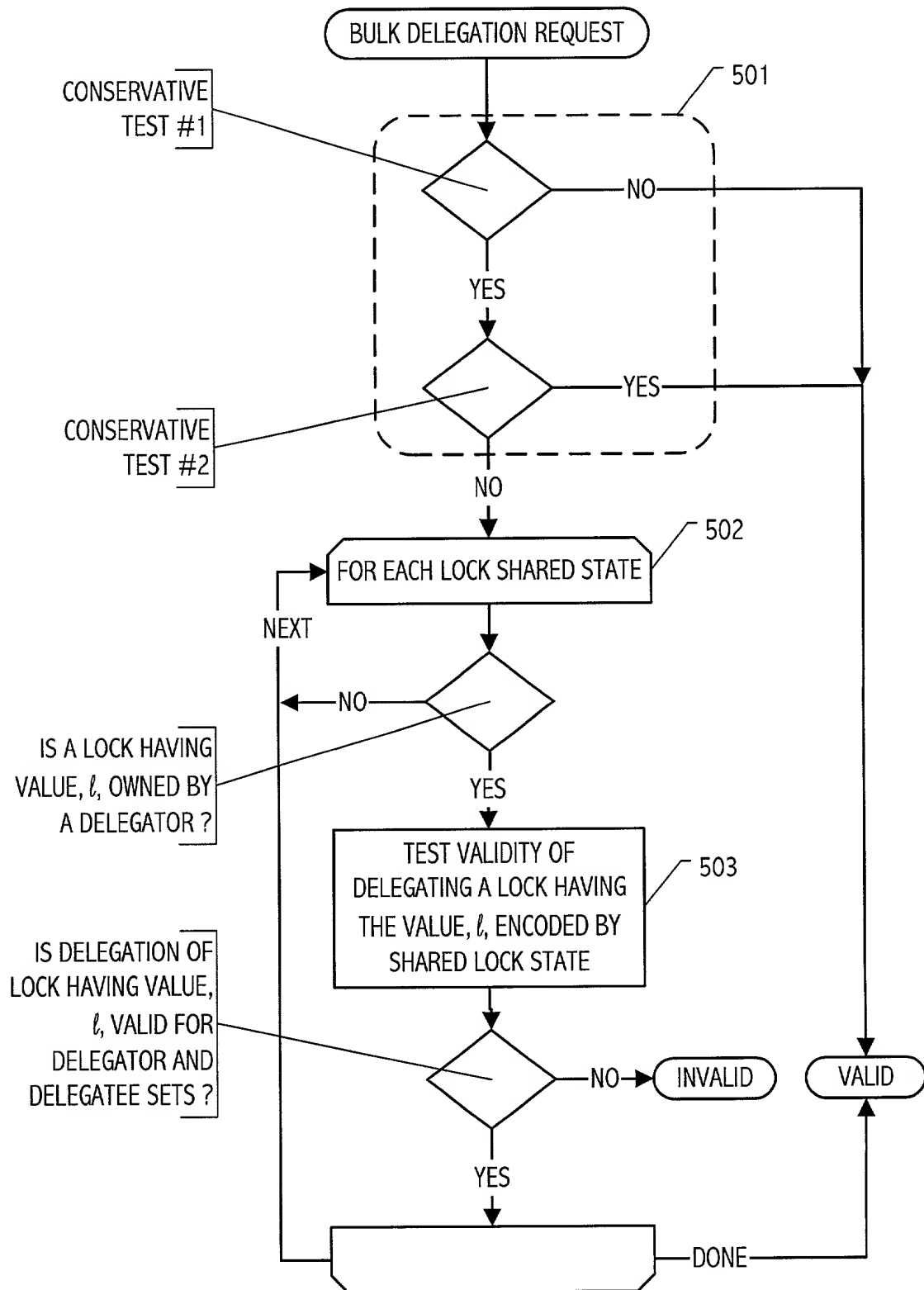


FIG. 5

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```
// Determine the validity of a bulk lock delegation
boolean isValid(delegators, delegates)
begin
  602 — if  $wset \cap delegates = \emptyset$ 
    return true
  603 — else if  $(\forall t_d \in delegates, \forall t_s \in delegators, \forall C \in \{rw, wr, ww\},$ 
    ( $ICW(t_s, C) - (delegators \cup \{t_d\}) \subseteq ICW(t_d, C)$ )
    // if at least one of the delegates lock is a write lock, the request
    // is valid only if the delegates can ignore all conflicts which each other
    if  $\exists l, Owners(l, Write) \cap delegators \neq \emptyset$ 
      return  $(\forall t \in delegates, \forall c \in \{rw, wr, ww\}, delegates \subseteq ICW(t, c))$ 
    else
      return true
    endif
  else
    // The two conservative tests have failed
    foreach l in TSLS
      if  $Owners(l, W) \neq \emptyset \wedge (\exists M, Owners(l, M) \cap delegators \neq \emptyset)$ 
        601 — if  $\neg isValid(delegators, delegates, l)$ 
          return false
        endif
      endif
    end
  endif
  return true
end
```

FIG. 6